

**Cooperative Scheme - An Alternative Approach to an Equitable and
Pareto-Improving Transportation System**

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1 ABSTRACT

2 We propose an alternative approach to an equitable and Pareto-improving transportation system based on
3 cooperation among travelers assisted by defector penalty. In the theoretical analysis, it is shown that when
4 the value of time (VOT) is bounded from above, a Pareto-improving cooperative scheme without financial
5 transactions always exists, in which case the defector penalty is high enough so that all travelers cooperate.
6 A more practical and potentially more appealing case is discussed where a certain number of defectors
7 exist while the travel time of cooperators is strictly better than that in UE. A mathematical programming
8 problem is formulated for the optimal cooperative scheme problem in a general network with Pareto-
9 improving constraints and practical considerations on the length the cooperation cycle. Computational
10 tests on a simple network and solutions are evaluated in terms of efficiency improvement (total system
11 travel time) and equitability (Gini index).

1 INTRODUCTION AND LITERATURE OVERVIEW

2 User Equilibrium (UE) is based on the assumption that travelers behave selfishly in a non-cooperative
3 manner to minimize their own travel cost. System Optimum (SO) is a traffic state where the total cost of
4 the system is minimized. However, SO is not stable as drivers on slow routes will likely shift to the fast
5 routes, and cause the system to revert back to UE. Therefore, drivers need to be penalized through charges
6 or compensated through rewards for the system to move towards SO. The study of congestion pricing is
7 traced back to the early twentieth century when (1) recommended a tax to be levied on any market activity
8 that generates negative externalities. (2) proposed a time-varying toll that could completely eliminate
9 queuing delay, and thereby maximize system efficiency. A plethora of studies have been conducted in this
10 area since then.

11 Despite its theoretical appeal, congestion pricing continues to be a hard sell to people. Major
12 proposals have been remonstrated by public or political opposition. For example, cordon tolling schemes
13 for Edinburgh and Manchester in the UK were rejected by public referenda (2005 and 2008). An online
14 petition to the UK government (2007) attracted more than 1.8 million signatures against road pricing, and
15 effectively put an end to plans for a national scheme in the UK for the time being. A cordon toll plan
16 for New York City was stopped by the New York state legislature (2008) when it declined to vote on the
17 proposal. These setbacks illustrate the difficulties of designing congestion pricing schemes that are both
18 efficient and publicly acceptable (3).

19 There are a wide range of factors for the setbacks, and equity is one of the most cited. Congestion
20 pricing sometimes is characterized as a “regressive tax” (4) in that high income travelers who usually have
21 a high value of time (VOT) could benefit at the cost of low income travelers’ loss. Innovative solutions
22 to the equity issue have focused on the so-called Pareto-improving schemes, where no traveler is worse
23 off compared to the no-toll case. Examples include a hybrid scheme between rationing and pricing (5,
24 6), alternating charging a given fraction of the drivers (7), Pareto-improving pricing (8), credit-based
25 scheme (9), tradable credit scheme (10–13), and toll-and-subsidy scheme (14–16).

26 The cooperative scheme (CS) proposed in this research is an extension of the hybrid scheme be-
27 tween rationing and pricing, first proposed by (5) for a single bottleneck with flexible demand, and later
28 adopted and extended by other researchers, e.g., (6). The major distinction is that the CS in this research
29 is applied to route choice in a general network, where the “rationing” is origin-destination (OD) and
30 route-specific. This flexibility allows for potentially more room for improvement in both efficiency and
31 equitability, but also renders a more challenging problem.

32 It is hypothesized that traveler cooperation will bring about transformative changes to how the
33 transportation system is managed (17), and its implementation can be accelerated by technologies includ-
34 ing connected and autonomous vehicles (CAV). Specifically, with fully autonomous vehicles, the barrier to
35 participation in the cooperative scheme due to cognitive constraint (e.g., inertia against regular switching
36 to potentially unfamiliar routes/departure time) and disruption to the execution due to human errors (e.g.,
37 failing to follow specified route) can be significantly reduced, and even eliminated.

38 As reviewed in (17), cooperation has been studied extensively in behavioral economics and game
39 theory to resolve social dilemmas such as Prison’s Dilemma (18). Evolutionary game theory provides a
40 competent theoretical framework for addressing the subtleties of cooperation in such situations (19–22).
41 (23) conducted experiments on humans playing two-person route choice games in a computer laboratory
42 to study decision behavior in repeated games. Results show that a taking-turn strategy that achieves SO
43 emerges after the two players have enough experience to perceive the value of cooperation. However,
44 computer simulations and additional experiments indicate that oscillatory cooperation in route choice
45 games with four players emerge only after a long time period (rarely within 300 iterations).

46 Almost all traffic equilibrium studies make the assumption that travelers are non-cooperative, for
47 a good reason. With the large number of travelers, the time it takes for cooperation to emerge is too long

1 for the assumption to be practically valid. Penalty to defectors (people who do not cooperate) has been
 2 suggested (17, 23) to promote cooperation. This study operationalizes the idea in both theoretical and
 3 computational analyses.

4 The remainder of the paper is organized as follows. The next section presents a theoretical analysis
 5 of the CS for both homogenous and heterogenous VOT. A mathematical formulation of the optimal CS
 6 problem is then presented along with computational tests. Finally conclusions and future directions are
 7 provided.

8 THEORETICAL ANALYSIS

9 Consider a single-OD network (Figure 1) with fixed demand d , connected by two routes: Fast Route with
 10 a travel time t_F at SO and Slow Route with a travel time t_S at SO. The two routes have the same travel
 11 time at UE, t^{UE} , and $t_F < t^{UE} < t_S$. x_F and x_S are the SO flows (positive integers) on Fast Route and Slow
 12 Route respectively, and $x_F + x_S = d$. Travel time is a strictly increasing function of flow.

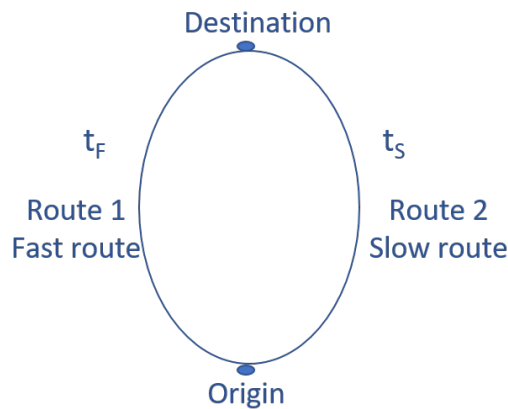


FIGURE 1 A single-OD two route network

13 A CS is defined as travelers taking turns to use Fast Route. Participants of the cooperative scheme
 14 are called “cooperators”. They use Fast Route on some days and Slow Route on other days following the
 15 guidance of a central controller to maintain an SO flow pattern on each day, even though the composition
 16 of the flow varies from day to day due to turn taking.

17 When all travelers are cooperators, a naive turn-taking strategy is such that in each cycle of d days,
 18 each cooperator uses Fast Route for x_F days and Slow Route for x_S days. The average travel time for each
 19 cooperator over a cycle is the average SO travel time:

$$t^{SO} = \frac{x_F t_F + x_S t_S}{d} \quad (1)$$

20 It is evident that $t_F < t^{SO} < t^{UE} < t_S$.

21 Such a scheme can be directly extended to multiple ODs and more than two routes per OD when
 22 all travelers are cooperators. For any OD (m, n) with demand d^{mn} , in a cycle of d^{mn} days, each cooperator
 23 uses the routes in proportion to the SO route flows (positive integers). Since SO flows are maintained
 24 for each OD, they must be maintained for the network, although the composition of the flows varies. In
 25 classical traffic assignment problems, flows are fractional numbers instead of integers, however, when the
 26 flow is large enough, the difference of rounding to integers is negligible (not to mention that flows are
 27 integers in reality).

1 A shorter cycle is preferred as it demonstrates the value of turn-taking in shorter time and thus more
 2 appealing for getting public acceptance. With an improved strategy, cooperators take turns by blocks. Let
 3 g be the greatest common factor of x_F and x_S . Cooperators are grouped into d/g blocks. In each cycle
 4 of d/g days, each block of cooperator uses Fast Route for x_F/g days and Slow Route for x_S/g days. The
 5 resulting average travel time over a cycle is still t^{SO} . In practical applications, the cycle length might need
 6 to be controlled below a fairly small number, say, 5 working days, to have a realistic chance of acceptance.
 7 In such cases, indifference to small travel time differences (e.g., a 5-minute difference for a 1-hour trip)
 8 can be exploited such that a small number of approximately equal-sized blocks result in approximately
 9 equal average travel time for each cooperator with the differences under a certain threshold. A turn taking
 10 strategy of a small number of blocks of cooperators is demonstrated in Figure 2. On day 1, blocks 1 and
 11 2 use the fast route. On day 2, block 2 switches to slow route and block 3 switches to fast route. And on
 12 day 3, block 1 and 2 interchanges their route. Thus each block of cooperator uses fast route for 2 days and
 13 slow route for 1 day.

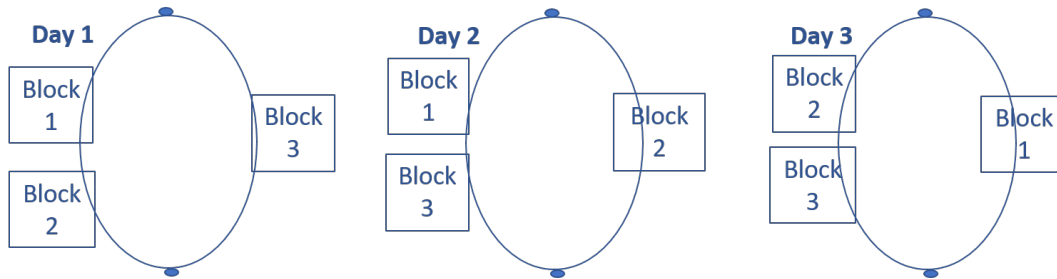


FIGURE 2 Turn-taking of 3 blocks of cooperators over a cycle of 3 days

14 The cooperative scheme is not stable, as a “defector” who stays on Fast Route all the time has
 15 a lower travel time of t_F than a cooperator. As more travelers defect, the cooperative scheme is broken
 16 and the system reverts back to UE. One way to maintain the cooperative scheme is to impose a defector
 17 penalty τ to make defection more costly than or at least as costly as cooperation.

18 Homogeneous VOT

19 If a single VOT of $\bar{\beta}$ is assumed for all the travelers, $\tau \geq \bar{\beta}(t^{SO} - t_F) = \bar{\beta}(t_S - t_F)x_S/d$.

20 When $\tau > \bar{\beta}(t_S - t_F)x_S/d$, defection is more costly than cooperation, and thus no defectors exist
 21 and no financial transactions.

22 When the penalty is exactly $\bar{\beta}(t_S - t_F)x_S/d$ and the penalty collected from defectors is distributed
 23 evenly to cooperators, defection is as costly as cooperation. Multiple cooperative schemes exist with
 24 different number of defectors, n , ranging from 0 to x_F . When $n = 0$, the cooperative scheme is the same
 25 as described above. When $0 < n < x_F$, cooperators have to use Fast Route proportionally less often than
 26 when $n = 0$ to maintain the SO flow pattern, and their average travel time

$$t^{CS}(n) = \frac{(x_F - n)t_F + x_S t_S}{d - n}. \quad (2)$$

27 $t^{CS}(n)$ is an increasing function of n , and $t^{CS}(n) > t^{CS}(0) = t^{SO}, \forall n > 0$. In other words, given that the total
 28 system travel time remains at the SO value, the reduction in travel time for defectors ($t_F < t^{SO}$) is at the
 29 cost of cooperators in terms of increased travel time. The increased travel time is compensated for by the
 30 re-distributed defector payment. It can be shown mathematically that defectors and cooperators have the
 31 same generalized cost (combining time and monetary costs) equal to t^{SO} (in time units). Intuitively, the
 32 payment is a transfer within the system and thus does not affect total system cost, which remains the SO

total travel time. The generalized costs of a defector and cooperator are equal as there are positive numbers of both (non-corner solution), and as a result, they must be equal to the average SO travel time. When $n = x_F$, the cooperative scheme degenerates to traditional congestion pricing with toll re-distribution, where no turn-taking is happening as Fast Route is filled up by defectors. Note that a cooperative scheme that does not maintain an SO flow pattern (but still better than UE in total travel cost) is still possible when $n = x_F$.

Heterogeneous VOT

Realistically, VOT is heterogeneous among travelers. Let β be the random VOT distributed over travelers. If the support of β has an upper bound $\check{\beta}$, it is trivial to show that a cooperative scheme (maintaining SO flow pattern) always exists with the defector penalty $\tau \geq \check{\beta}(t_S - t_F)x_S/d$. This is a much milder condition compared to those for Pareto-improving congestion pricing with toll re-distribution [16]. An added advantage, as mentioned previously, is that no financial transactions are needed and thus the dooming perception of “tax” is avoided.

Practical considerations might lead to an upper bound on the defector penalty, for example, to avoid the perception of forced cooperation with the government. When $\tau < \check{\beta}(t_S - t_F)x_S/d$, a traveler with the threshold VOT, $\check{\beta} = (1/\tau)(t_S - t_F)x_S/d$, is indifferent between cooperation and defection. Travelers with a VOT higher than $\check{\beta}$ will defect while those with a VOT lower than $\check{\beta}$ will cooperate. The existence condition of the scheme is thus a condition to ensure that the number of defectors is no larger than x_F . With the same re-distribution scheme, it can be shown that every traveler is better off compared to UE¹, although the generalized cost is not equalized among travelers due to heterogeneous VOT.

A potentially more appealing scheme is to set the penalty to a value high enough but not too high, so that a certain number of defectors exist while the travel time of cooperators is strictly better than that in UE. It appeals to high-VOT travelers by giving them an option to pay for better travel time; it appeals to low-VOT travelers by reducing their travel time and on top of that, providing monetary rewards (re-distributed defector penalty). The overall scheme would thus be less likely viewed as authoritarian. The number of defectors to ensure a strictly improving travel time for cooperators is such that

$$n < \frac{x_F(t_S - t_F) - d(t_S - t^{UE})}{t^{UE} - t_F}. \quad (3)$$

Under the condition that $x_F(t_S - t_F) > d(t_S - t^{UE})$, such an n always exists. Let $F_\beta(\cdot)$ be the cumulative distribution function of β . The penalty corresponding to a given number of defectors n is $F_\beta^{-1}(\frac{d-n}{d})(t_S - t_F)x_S/d$.

A MATHEMATICAL PROBLEM FORMULATION FOR OPTIMAL CS IN A GENERAL NETWORK

The naive CS in the previous section cannot be applied to a real network, as the cycle length must be short enough to gain public acceptance. Integer non-linear programming problem formulations are proposed to

¹The traveler with threshold VOT, $\check{\beta}$, has a generalized cost of t^{SO} that is strictly better than t^{UE} . S/he can serve as a reference for a regular defectors or cooperators whose VOT is different from $\check{\beta}$. A regular defector has a higher VOT and the same travel time as the threshold defector. It follows that the travel time saving $t^{UE} - t_F$ is more valuable than for the threshold defector in terms of offsetting the penalty. The threshold defector is better off and thus the regular defector is also better off. A regular cooperator has a lower VOT and the same travel time as the threshold cooperator. When the regular cooperator's travel time is lower than that in UE, s/he is better off since the re-distributed penalty can only further reduce the generalized cost. When the regular cooperator's travel time is higher than that in UE, the increase in travel time is less detrimental than for the threshold cooperator in terms of offsetting the re-distributed penalty. The threshold cooperator is better off and thus the regular cooperator is also better off.

1 find optimal CS in a general network with a given cycle length.

2 **Formulation 1**

3 Let L be the set of links in the network, I^{mn} the set of travelers (all assumed to be cooperators) between
 4 OD pair (m, n) and D the fixed cycle length. $t_a(\cdot)$ is the volume-delay function on link a as a function of
 5 the flow on link a . A binary variable, x_{adi}^{mn} is defined to indicate whether a traveler is on a particular link
 6 on a given day.

$$7 \quad x_{adi}^{mn} = \begin{cases} 1, & \text{if individual 'i' of OD pair (m,n) is on link 'a' on day 'd'} \\ 0, & \text{otherwise} \end{cases}$$

8 The average daily total travel time of the system $Z(x)$, is calculated as

$$Z(x) = \sum_d \sum_a t_a \left(\sum_{mn,i} x_{adi}^{mn} \right) \sum_{mn,i} x_{adi}^{mn} / D \quad (4)$$

9 We set up a set of equity constraints to ensure that the CS is equitable to the cooperators.

$$|\frac{1}{D} \sum_d \sum_a t_a \left(\sum_{mn,i} x_{adi}^{mn} \right) x_{adi}^{mn} - u^{mn}| \leq \epsilon u^{mn}, \forall (m, n), \forall i \in I^{mn} \quad (5)$$

10 where

$$u_{mn} = \frac{1}{D * |I^{mn}|} \left(\sum_d \sum_a t_a \left(\sum_{mn,i} x_{adi}^{mn} \right) \sum_{mn,i} x_{adi}^{mn} \right) \quad (6)$$

11 Equation 5 ensures that differences of average travel time among cooperators over a cycle falls
 12 within a certain threshold (e.g. 5%). u_{mn} is the average travel time between OD (m, n) over a cycle.

$$\sum_{a \in A(m)} x_{adi}^{mn} = 1, \forall (m, n), \forall i, \forall d \quad (7)$$

$$\sum_{a \in B(n)} x_{adi}^{mn} = 1, \forall (m, n), \forall i, \forall d \quad (8)$$

$$\sum_{a \in A(k)} x_{adi}^{mn} = \sum_{a \in B(k)} x_{adi}^{mn}, \forall k \neq m, n, \forall i, \forall d \quad (9)$$

13 Equations 7 through 9 are the flow conservation constraints. Equation 7 implies that the flow out
 14 of an origin (m) has to be exactly equal to 1 for any person (i) on any given day (d). Equation 8 implies
 15 that the flow incoming to a destination (n) has to be exactly equal to 1 for any person (i) on any given day
 16 (d). Equation 9 implies that the inflow is equal to outflow at any intermediate node for any person(i) on
 17 any given day(d).

18 Therefore, the cooperative scheme is formulated as a constrained non-linear optimization problem,

$$\begin{aligned} \mathbf{P1} \quad & \min_{x_{adi}^{mn}} \quad Z(x) \\ & \text{s.t.} \quad \text{Eqs. (5) - (9)} \\ & \quad \quad x \in \{0, 1\} \end{aligned}$$

1 Formulation 2

2 The above formulation is an integer non-linear programming problem which is difficult to solve due to the
 3 combination of non-convexity of Eq. (5) and the integrality constraints. We implemented a Lagrangian
 4 relaxation algorithm to solve the problem and tested it in small problem instances using Matlab. However
 5 the efficiency and effectiveness of the algorithm is still a major concern and thus an alternative formation
 6 is proposed that replaces the equity constraints (Eq. 5) with Pareto-improving constraints.

$$\frac{1}{D} \sum_d \sum_a t_a \left(\sum_{mn,i} x_{adi}^{mn} \right) x_{adi}^{mn} \leq t^{UE}, \forall (m,n), \forall i \in I^{mn} \quad (10)$$

7 where the the average travel time of cooperators over a cycle is on greater than the UE travel time for any
 8 OD.

9 Formulation 2 is as follows:

$$\begin{aligned} \mathbf{P2} \quad & \min_{x_{adi}^{mn}} \quad Z(x) \\ & s.t. \quad Eqs.(10), (7) - (9) \\ & \quad \quad x \in \{0, 1\} \end{aligned}$$

10 COMPUTATIONAL TESTS

11 P2 is easier to solve in that constraint (10) is convex. However the number of integer decision variables,
 12 which is the product of the total demand (integer), cycle length and number of links, makes the problem
 13 still difficult. A similar strategy as in the theoretical analysis is adopted where the travelers are divided
 14 into groups with approximately the same size, and the binary decision variables are defined for groups
 15 instead of individuals.

16 We used BONMIN (Basic Open-source Nonlinear Mixed INteger programming) which is an open-
 17 source C++ code for solving general MINLP (Mixed Integer NonLinear Programming), run remotely
 18 through the NEOS web interface.

19 We tested P2 in a single-OD two-route network with the following volume-delay functions:

$$20 \quad t_1 = 2 + \left(\frac{x_1}{3000}\right)^2, \quad t_2 = 12 + \frac{x_1}{3000}$$

21
 22 Sensitivity analysis is done by starting with a demand of 9000 users and then scaling it in the range
 23 of 0.5 to 1.5. Different group sizes ranging from 3 to 5 and cycle lengths in the range of 3 to 5 are also
 24 tested.
 25

26 Table 1 shows the optimal turn taking strategy for 9000 users divided into three groups. It can be
 27 seen that three groups of cooperators achieve the SO flow pattern by taking turns within a cycle length
 28 of 3 days. With increased cycle length of 4 and 5 days respectively the resulting average travel times are
 29 still close to SO and Pareto-improving for each groups. The defector penalty is calculated by taking the
 30 difference between a free riders (defector) travel time and the highest average travel time of a cooperator.
 31 A constant VOT of 50\$/hr is considered for calculating the defector penalty.

32 Figure 3 shows a barplot of average travel time of 3 groups of cooperators at a demand level 9000.

33 The red horizontal line in Figure 3 represents the UE travel time. It can be seen that each group of
 34 cooperators for this demand level has strictly better travel time than UE.

35 In order to evaluate the efficiency and equity standard of the cooperative scheme we used two
 36 matrices: % of maximum travel time improvement (% Max), defined as the difference in average travel
 37 time between UE and SO, and the GINI coefficient (0 indicates perfect equity, and 1 inequity). Table
 38 2 shows that when demand is low (4500 and 6750), SO and UE are the same and there is no room for

TABLE 1 Optimal Cooperative Scheme for a demand of 9000 users divided into 3 groups

	Link 1			Link 2			Flow on link 1	Flow on link 2	Defector penalty,\$
	Group 1	Group 2	Group 3	Group 1	Group 2	Group 3			
Day 1	1	0	1	0	1	0	2	1	1.94
Day 2	1	1	0	0	0	1	2	1	1.94
Day 3	0	1	1	1	0	0	2	1	1.94
# of Days on Link	2	2	2	1	1	1			
Day 1	1	0	0	0	1	1	1	2	3.75
Day 2	0	1	1	1	0	0	2	1	3.75
Day 3	0	1	1	1	0	0	2	1	3.75
Day 4	1	1	0	0	0	1	2	1	3.75
# of Days on Link	2	3	2	2	1	2			
Day 1	1	1	0	0	0	1	2	1	4.17
Day 2	0	1	1	1	0	0	2	1	4.17
Day 3	1	0	0	0	1	1	1	2	4.17
Day 4	1	0	1	0	1	0	2	1	4.17
Day 5	1	0	1	0	1	0	2	1	4.17
# of Days on Link	4	2	3	1	3	2			

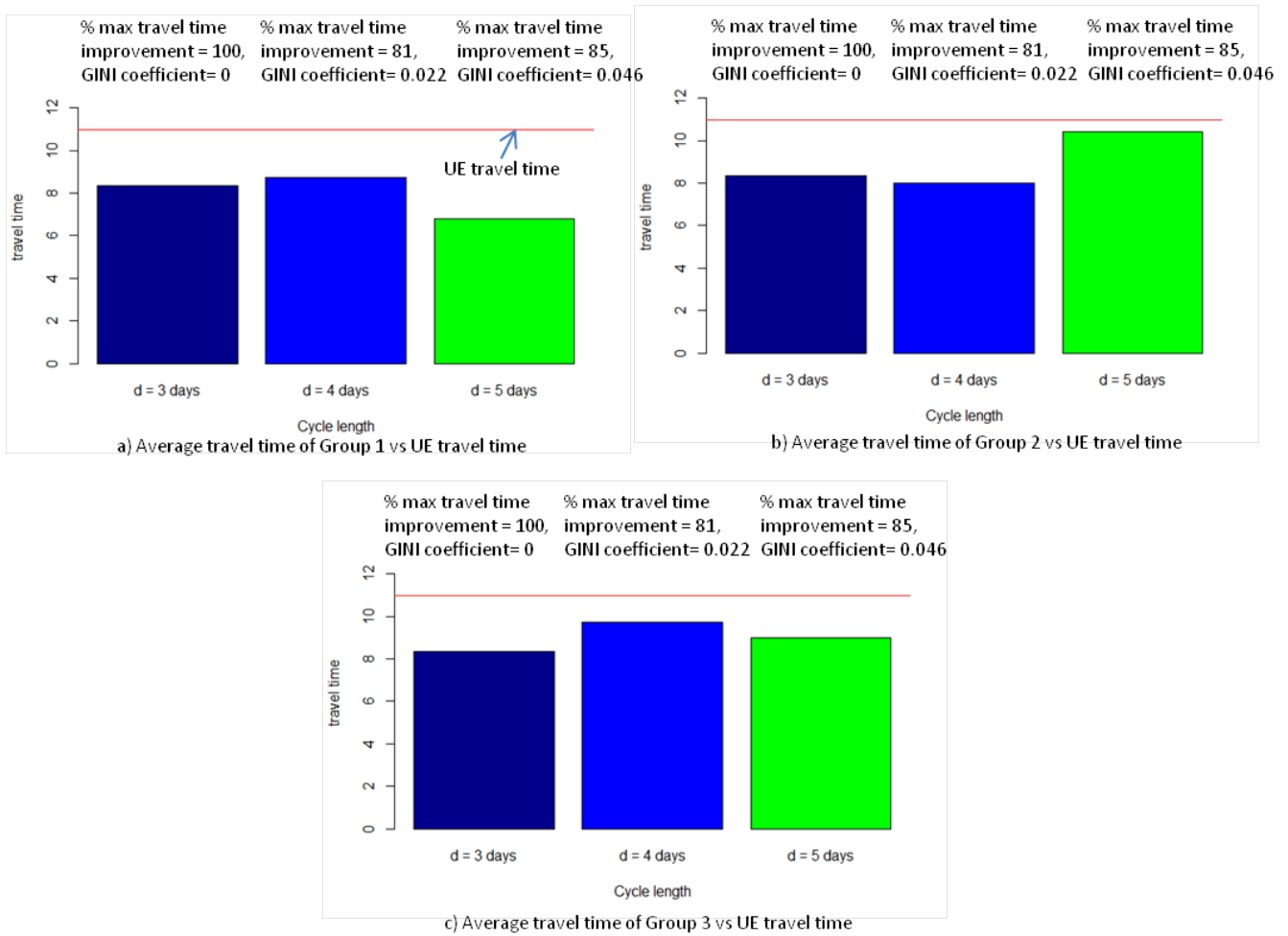


FIGURE 3 Average travel time of 3 groups of cooperators over different cycle length

1 improvement. When the demand is high enough to create efficiency difference between SO and UE, it
 2 seems that the higher the demand, the smaller the possible gain from turn taking. GINI indices in all cases
 3 are fairly small and achieves 0 with 3 groups, indicating that the equity issue is well accounted for. Table
 4 3 shows that a larger number of groups generally improves both the efficiency and equity of the CS, which
 5 is reasonable given that a larger number of groups allows for more flexibility in the turn-taking.

TABLE 2 Performance metrics at different demand level and cycle lengths (3 groups)

Cycle length (day)	Demand = 4500		Demand = 6750		Demand = 9000		Demand = 11250		Demand = 13500	
	% Max	GINI	% Max	GINI	% Max	GINI	% Max	GINI	% Max	GINI
3	0	0	0	0	100	0	89	0	69	0
4	0	0	0	0	81	0.022	89	0.014	69	0.026
5	0	0	0	0	85	0.046	89	0.034	69	0.021

TABLE 3 Performance metrics with different group sizes and cycle lengths (demand = 9000)

Cycle length (day)	Number of Groups = 3		Number of Groups = 4		Number of Groups = 5	
	% Max	GINI	% Max	GINI	% Max	GINI
3	100	0	96	0.021	96	0.063
4	81	0.022	96	0.031	96	0.028
5	85	0.046	96	0.029	96	0

6 CONCLUSIONS AND FUTURE DIRECTIONS

7 This research extends the rationing and pricing scheme to a general network to cope with the equity issue
 8 when driving a transportation system from UE to SO. In the theoretical analysis, it is shown that when
 9 the value of time (VOT) is bounded from above, a Pareto-improving cooperative scheme without financial
 10 transactions always exists, in which case the defector penalty is high enough so that all travelers cooperate.
 11 A more practical and potentially more appealing case is discussed where a certain number of defectors
 12 exist while the travel time of cooperators is strictly better than that in UE. A mathematical programming
 13 problem is formulated for the optimal cooperative scheme problem in a general network with Pareto-
 14 improving constraints and practical considerations on the length the cooperation cycle. Computational
 15 tests on a simple network and solutions are evaluated in terms of efficiency improvement (total system
 16 travel time) and equitability (Gini index).

17 Future research directions include 1) systematic testing of the CS as formulated (P2) in realistic
 18 networks, 2) extension of the analysis to probabilistic route choice so that stochastic UE (SUE) emerges
 19 without interventions, and 3) extension of the formulation to allow a certain fraction of defectors so that
 20 the system will not be viewed as too authoritarian.

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